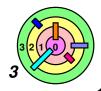
# 5.3 Scheduling

- Goals
- Scheduling Algorithms
- | Implementation Issues
- **Case Studies**



# Scheduling Algorithms

**Priority** Basic

Multi-level FIFO

→ SRTN

- RR

**Prortional Share** 

Lottery

SJF → Multi-level → Stride\*

**Real Time** 

EDF

Rate

**Monotonic** 



We will focus on how the run queue is managed



All these schedulers are work-conserving

w/ Feedback\*

- if there is work to be perform, must keep CPU busy
- opposite of "vacationing scheduler"

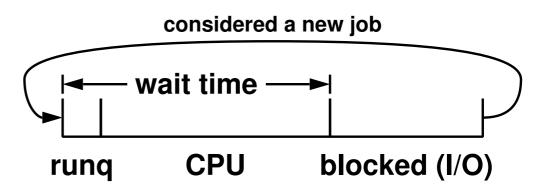


# Scheduling Non-preemptive, Non-interactive Jobs



### Scheduling "jobs"

wait time is over when job voluntarily gives up the CPU





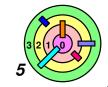
#### Run one at a time

- no preemption



### Running time is *known*

- $\rightarrow$  jobs  $J_i$  with processing/execution time  $T_i$  for i = 0, 1, 2, ...
- not realistic
  - if you know the running time of every job, what would you do?



# **FIFO**





Ex: weenix



# **Performance Metric: Throughput**



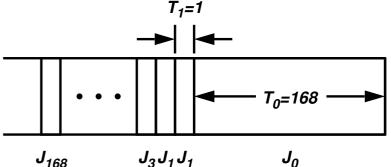
"Goodness" criterion is jobs/hour

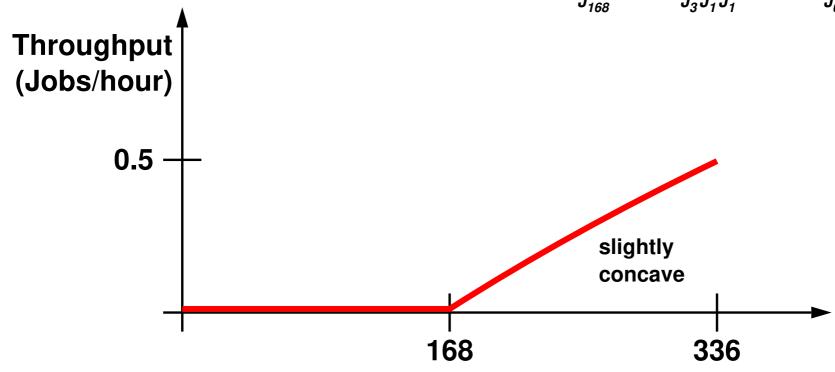
assuming that all jobs are sitting in the run queue at time 0



#### Ex:

- one 168-hour job
- followed by 168 one-hour jobs







# **Another Performance Metric: Average Wait Time**



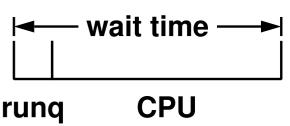
Jobs  $J_i$  with processing/execution time  $T_i$  for  $0 \le i < n$ 



Average wait time (AWT) for FIFO

- please note that this is not the same as any warmup2 "wait time"
- $J_i$  started at time  $t_i$

$$- t_i = \sum_{j=0}^{i-1} T_j \text{ (for FIFO)}$$



 $WT_i = t_i + T_i$  (for non-preemptive schedulers)

$$\Rightarrow$$
  $AWT = \sum_{i=0}^{n-1} WT_i / n = \sum_{i=0}^{n-1} (t_i + T_i) / n$ 



For our example (which is the worst-case for FIFO)

- **→** AWT = *252* hours (with a standard deviation of *48.79* hours)
  - large average and large variation (for this example)



In general, AWT for FIFO is more difficult to compute

 need to look at all possible ordering of jobs and the probability of getting each particular order



### **Shortest Job First**



How to *minimize* AWT?

$$AWT = \sum_{i=0}^{n-1} (t_i + T_i) / n$$

$$- t_i = \sum_{j=0}^{i-1} T_j$$

if 
$$i > 0$$
,  $t_i = T_{i-1} + t_{i-1}$ 



$$AWT = (nT_0 + (n-1)T_1 + (n-2)T_2 + ... + 2T_{n-2} + T_{n-1}) / n$$

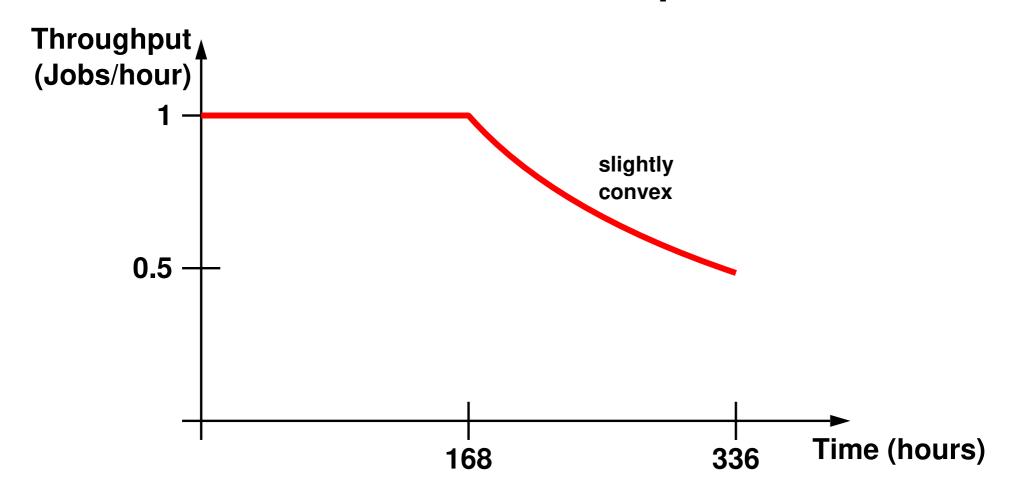


Minimized when  $T_i \leq T_{i+1}$  for all i

which is Shortest Job First (SJF)



# SJF and Our Example

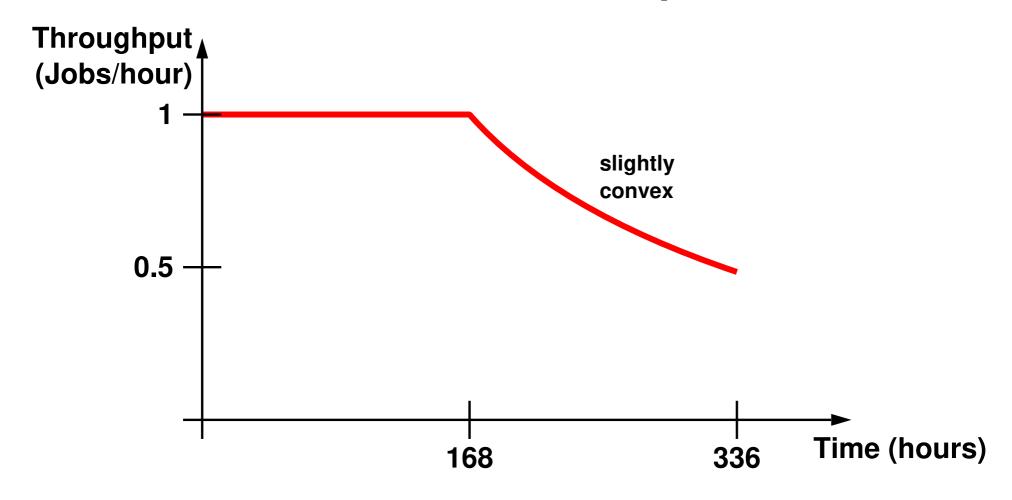


**→** AWT = *85.99* hours (with a standard deviation of *52.06* hours)



but throughput at time = 336 is identical for all work-conserving schedulers

# SJF and Our Example

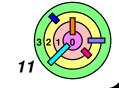


**→** AWT = *85.99* hours (with a standard deviation of *52.06* hours)



What if short jobs keep arriving?

- starvation
  - unacceptable for a scheduling policy

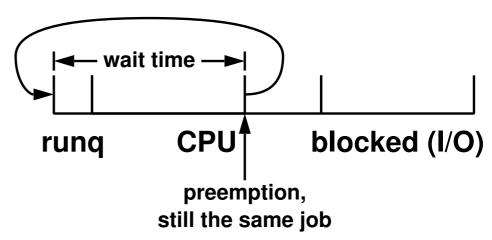


# Scheduling Preemptive, Non-interactive Jobs

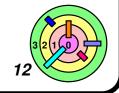


#### **Preemption:**

- current job may be preempted by others
  - if it goes to the runq due to preemption, it's still the same job



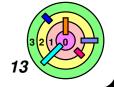
- it doesn't have to go to the tail of the runq
- wait time is the time when this job volunterily gives up the CPU minus the time it first entered the runq
- to minimize AWT, use shortest remaining time next (SRTN)
  - basically SJF
    - same argument that SJF minimizes AWT when there is no preemption
  - we reserve the term "SJF" to refer to the non-preemptive case



# **Fairness**

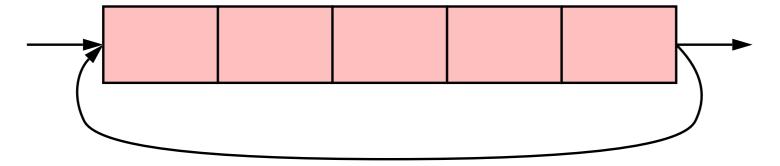


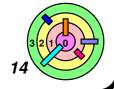
- each job eventually gets processed
- that seems fair
- SJF and SRTN
  - a long job might have to wait indefinitely
- What's a good measure of fairness?



Time-slicing

-q = quantum or time slice

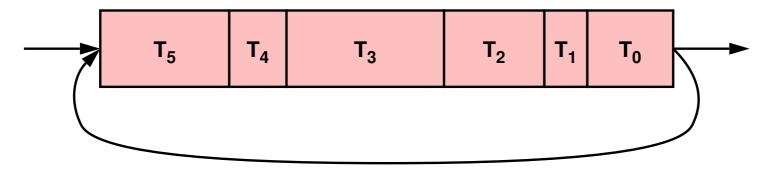


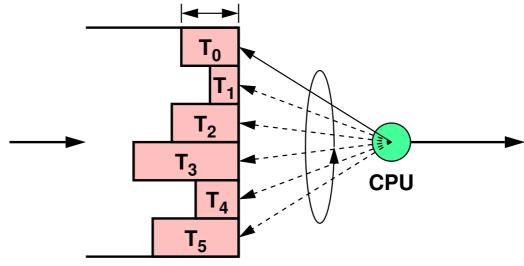


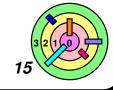


# **Time-slicing**

-q = quantum or time slice



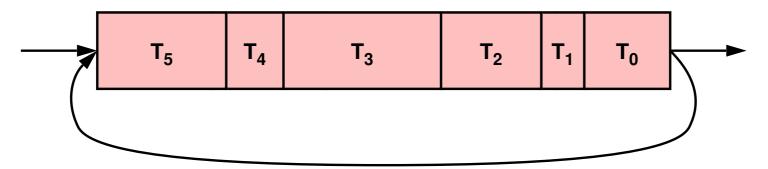






### **Time-slicing**

-q = quantum or time slice





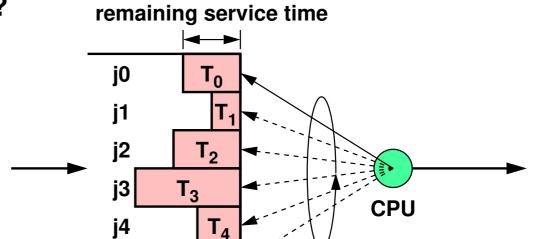
#### Different values of q

- ightharpoonup q 
  ightarrow 0: processor-sharing (idealized case)
  - not realistic
  - translation lookaside buffer flushing and caching problem
    - not enough time to achieve good hit-rate in TLB
- q too large: some jobs appear to be not making progress



How to calculate waiting time?

$$\longrightarrow$$
  $WT_1 =$ 



**T**<sub>5</sub>

j5

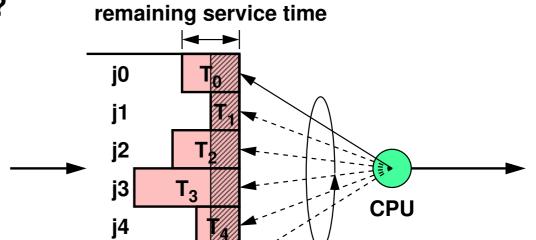


j5



$$\longrightarrow WT_1 = 6 \times T_1$$

- why not  $6 \times T_1 4 \times q$
- o  $q \rightarrow 0$ , we are doing calculus, not algebra





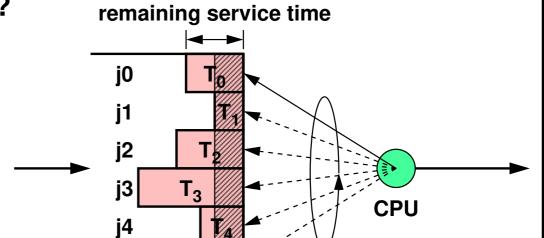
j5



How to calculate waiting time?

$$-WT_1 = 6 \times T_1$$

$$-WT_4 = ?$$



 $-\mathsf{T_4}-\mathsf{T_1}$ 

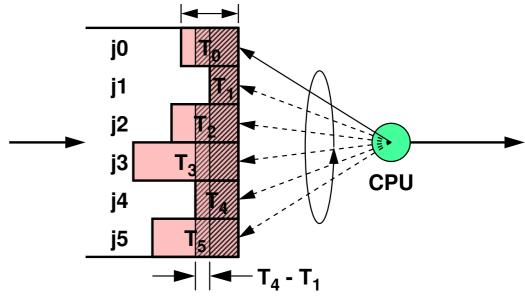


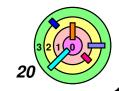


$$\longrightarrow$$
  $WT_1 = 6 \times T_1$ 

$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$







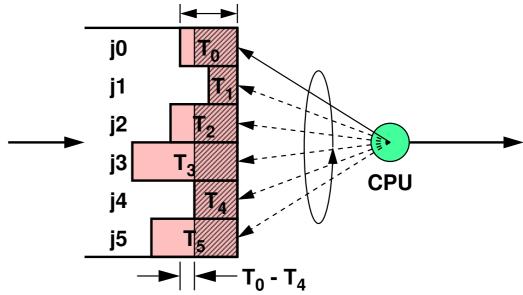


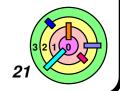
$$\longrightarrow WT_1 = 6 \times T_1$$

$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

$$\rightarrow WT_0 = ?$$







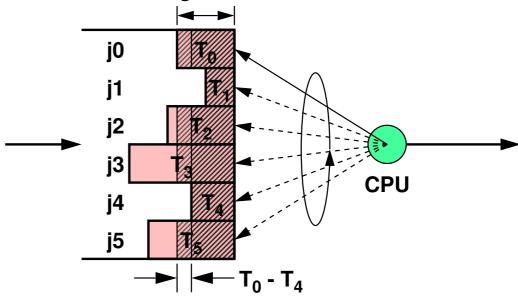


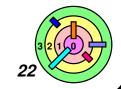
$$\longrightarrow$$
  $WT_1 = 6 \times T_1$ 

$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

$$WT_0 = 4 \times (T_0 - T_4) + WT_4$$









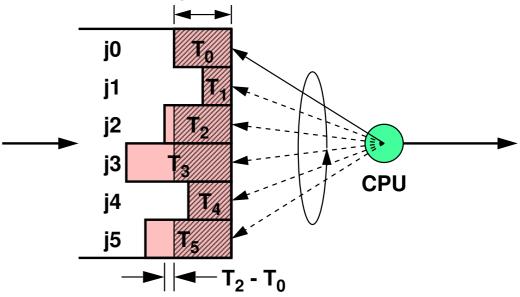
$$\longrightarrow$$
  $WT_1 = 6 \times T_1$ 

$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

$$WT_0 = 4 \times (T_0 - T_4) + WT_4$$

$$\longrightarrow$$
  $WT_2 = ?$ 









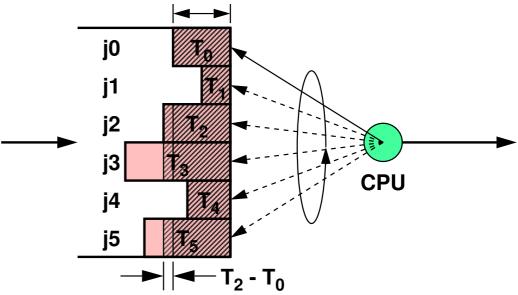
### How to calculate waiting time?

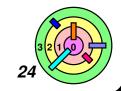
$$\longrightarrow WT_1 = 6 \times T_1$$

$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

$$WT_0 = 4 \times (T_0 - T_4) + WT_4$$

$$WT_2 = 3 \times (T_2 - T_0) + WT_0$$







### How to calculate waiting time?

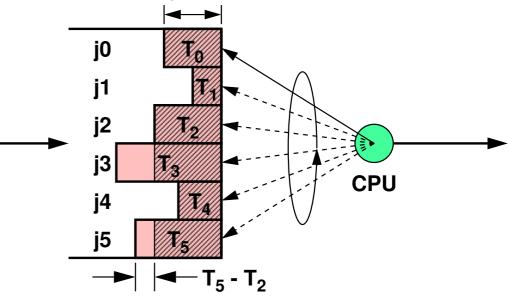
$$\longrightarrow WT_1 = 6 \times T_1$$

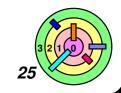
$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

$$WT_0 = 4 \times (T_0 - T_4) + WT_4$$

$$-WT_2 = 3 \times (T_2 - T_0) + WT_0$$

$$-WT_5 = ?$$







### How to calculate waiting time?

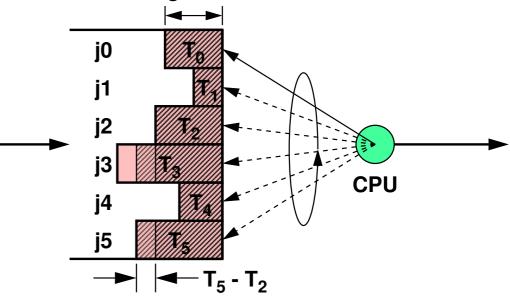
$$\longrightarrow WT_1 = 6 \times T_1$$

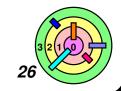
$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

$$WT_0 = 4 \times (T_0 - T_4) + WT_4$$

$$WT_2 = 3 \times (T_2 - T_0) + WT_0$$

$$-WT_5 = 2 \times (T_5 - T_2) + WT_2$$







#### How to calculate waiting time?

$$\longrightarrow$$
  $WT_1 = 6 \times T_1$ 

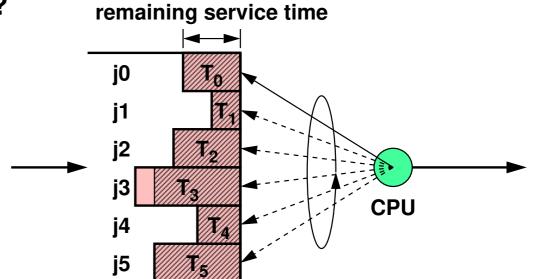
$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

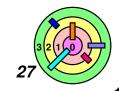
$$WT_0 = 4 \times (T_0 - T_4) + WT_4$$

$$WT_2 = 3 \times (T_2 - T_0) + WT_0$$

$$-WT_5 = 2 \times (T_5 - T_2) + WT_2$$

 $-WT_3 = ?$ 







### How to calculate waiting time?

$$\longrightarrow$$
  $WT_1 = 6 \times T_1$ 

$$WT_4 = 5 \times (T_4 - T_1) + WT_1$$

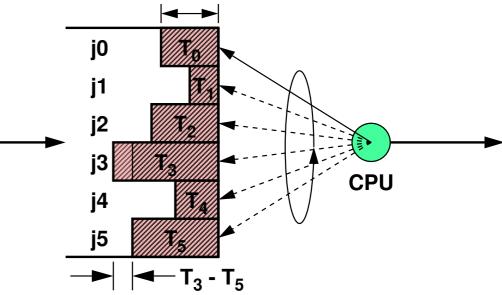
$$\longrightarrow WT_0 = 4 \times (T_0 - T_4) + WT_4$$

$$WT_2 = 3 \times (T_2 - T_0) + WT_0$$

$$-WT_5 = 2 \times (T_5 - T_2) + WT_2$$

$$-WT_3 = 1 \times (T_3 - T_5) + WT_5$$







#### Does it check out?

$$-WT_3 = T_0 + T_1 + T_2 + T_3 + T_4 + T_5$$



### Round Robin + FIFO



#### **AWT?**

- let quantum approach 0 (and pretend that it's realistic)
- 169 jobs sharing the processor
- run at 1/169th speed for first week
- short jobs receive one hour of processor time in 169 hours
  - different from SJF since all short jobs finish at about the same time
- long job completes in 336 hours
- **AWT** = *169.99* hours
  - recall that AWT is 252 hours for FIFO in our example and 85.99 hours for SJF
- → average deviation = 12.81 hours
  - recall that average deviation = 48.79 hours for FIFO in our example and 52.06 hours for SJF



RR + FIFO appears to be "fair"

no starvation

